

## Statistical Analysis Methods

The quantities reported in the Data Report are calculated in accordance with ASTM Standard E799-92, "Standard Practice for Determining Data Criteria and Processing for Liquid Drop Size Analysis".

## Explanation Of Terms Used On Droplet Size Reports

### Graphs

- Diameter Distribution :** a histogram of counts in the size classes; also called *number distribution*.
- Volume Distribution:** a histogram of the volume (in  $\mu\text{m}^3$ ) represented by the counts in each size class.
- Area Distribution:** a histogram of the area (in  $\mu\text{m}^2$ ) represented by the counts in each size class.
- Cumulative Volume:** a histogram of the total volume (in  $\mu\text{m}^3$ ) represented by the counts in all size classes below a given size class.

### Sample Analysis Summary (*diameters in $\mu\text{m}$* )

- Means:** [Diameter means are calculated based on the discrete particle diameters and counts]
- Arithmetic mean:** the average diameter on a simple numerical basis (**D10**):
- $$D_{10} = \left[ \frac{1}{N} \sum_{i=1}^N D_i \right]$$
- Surface mean:** the diameter of a drop whose surface area, if multiplied by the total number of droplets, will equal the total surface area of the sample (**D20**):
- $$D_{20} = \left\{ \frac{1}{N} \sum_{i=1}^N D_i^2 \right\}^{1/2}$$
- Volume mean:** the diameter of a drop whose volume, if multiplied by the total number of droplets, will equal the total volume of the sample. (**D30**):
- $$D_{30} = \left\{ \frac{1}{N} \sum_{i=1}^N D_i^3 \right\}^{1/3}$$
- Sauter mean:** the diameter of a drop whose area to volume ratio is the same as that of the entire sample (**D32**):
- $$D_{32} = \left[ \frac{\sum_{i=1}^N D_i^3}{\sum_{i=1}^N D_i^2} \right]$$

**Generalized mean diameter:**

$$D_{np} = \left\{ \frac{\sum_{i=1}^N D_i^n}{\sum_{i=1}^N D_i^p} \right\}^{1/(n-p)}$$

Volume percentiles: [Volume percentiles are based on the data after processing into the Class Table. The representative diameter for each class is the mid-point of the bin range.]

**DV01 :** the diameter such that the collection of drops whose diameter is below this value represents 10% of the sample volume

**DV05 :** the diameter such that the collection of drops whose diameter is below this value represents 50% of the sample volume

**DV09 :** the diameter such that the collection of drops whose diameter is below this value represents 90% of the sample volume

**Relative span :**

$$Span = \left[ \left\{ \frac{(D_{V0.9} - D_{V0.1})}{D_{V0.5}} \right\} 100\% \right]$$

**System Performance Summary**

**Validation**

**Attempted:** The number of samples attempted during data acquisition

**Validated:** The number of samples fulfilling the validation requirements during data acquisition

**Validation Rate:** The ratio of *Validated* to *Attempted* samples

**Data Rate :** average rate of attempted and validated samples

**Elapsed Time:** Total elapsed time measured from when data acquisition is started and terminated at each individual location, adjusted for deadtime settings.

**Velocity**

[Velocity statistics are based on the discrete particle velocity data]

**Mean:** The mean particle axial velocity weighted for residence time:

$$\bar{U}_{\text{weighted}} = \frac{\sum_i^N U_i D_{t_i}}{\sum_i^N D_{t_i}}$$

**Variance:**

The variance of the velocity weighted for residence time:

$$S^2_{\text{weighted}} = u^2 = \frac{\sum_i^N (U_i - \bar{U})^2 Dt_i}{\sum_i^N Dt_i}$$

**RMS:**

The RMS value calculated using the weighted variance:

$$s = \sqrt{u^2}$$

**Skewness:**

$$S_{\text{weighted}} = u^3 = \frac{\sum_i^N (U_i - \bar{U})^3 Dt_i}{s^3 \sum_i^N Dt_i}$$

**Flatness factor:**

$$K_{\text{weighted}} = u^4 = \frac{\sum_i^N (U_i - \bar{U})^4 Dt_i}{s^4 \sum_i^N Dt_i}$$

Sample [Sample statistics are based on the discrete particle data]

**Variance of diameter:**

$$s^2 = \int_{D_0}^{D_m} n(D)(D - D_{10})^2 dD$$

expanding this yields:

$$s^2_n = D_{20}^2 - D_{10}^2$$

**Skewness of diameter:**

$$S_n = \int_{D_0}^{D_m} n(D)(D - D_{10})^3 dD / s^3_n$$

expanding this yields:

$$S_n = (D_{30}^3 - D_{10}(D_{10}^2 + 3s^2_n)) / s^3_n$$

**Concentration:**

After correcting for cross-sectional bias, the size histogram is integrated with respect to diameter to produce the concentration [particles/cc].

**Volume Flux:**

The volume of dispersed phase crossing the measurement volume per unit time per unit area [cc/sec/cm<sup>2</sup>].

**Void fraction:**

$$vf = \left[ \frac{\sum_{i=1}^N \Delta t_i}{T} \right]$$

where:

$T$  is the duration of block during which  $N$  samples occur.

**Volume fraction:**

The percent volume of dispersed phase to carrier phase.

$$Vf = \left[ \left( \frac{p}{6} \right) \left( \frac{(D_{10})^3}{V} \right) \right]$$

where:

$V$  is the measurement volume size.

**Turbulence energy:**

$$T = \left[ \left( \frac{S}{U} \right) 100 \right]$$

### Statistical Definitions of Quantities Reported in Drop Size Distribution Table

**Count:** Straight count of the number of drops in the sample falling into that bin.

**Percentage occurrence:** The ratio of the number of drops in the  $i^{th}$  bin to the total number of drops in the sample:

$$\left[ \frac{n_i}{N} \right]$$

**Percent surface area:** The ratio of the sum of the squares of the diameters for all drops in the  $i^{th}$  bin to the same sum for all drops in the sample:

$$\left[ \frac{\sum_{n=i} D_n^2}{\sum_{n=0}^N D_n^2} \right]$$

**Area:** The total surface area [ $\mu\text{m}^2$ ] associated with the droplets contained within the  $i^{th}$  bin.

$$A_i = \left[ p \sum D_i^2 \right]$$

**Cumulative area:** The total surface area [ $\mu\text{m}^2$ ] associated with the droplets contained within all bins up to the  $i^{th}$  bin.

$$A_{cum_i} = \left[ p \sum_{n=0}^i D_n^2 \right]$$

**Volume:** The total volume [ $\mu\text{m}^3$ ] associated with the droplets contained within the  $i^{\text{th}}$  bin.

$$V_i = \left[ \frac{\rho}{6} \sum D_i^3 \right]$$

**Cumulative volume:** The total volume [ $\mu\text{m}^3$ ] associated with the droplets contained within all bins up to the  $i^{\text{th}}$  bin.

$$V_{cum_i} = \left[ \frac{\rho}{6} \sum_{n=0}^i D_n^3 \right]$$

**Percent volume:** The ratio of the sum of the cubes of the diameters for all drops in the  $i^{\text{th}}$  bin to the same sum for all drops in the sample:

$$\% V_i = \left[ \frac{\sum D_i^3}{\sum_{n=0}^N D_n^3} \right]$$

**Cumulative volume percent:** A running total of the percent volume for all bins up to the  $i^{\text{th}}$  bin.

$$\% V_{cum_i} = \left[ \frac{\sum_{n=0}^i D_n^3}{\sum_{n=0}^N D_n^3} \right]$$